



8. If  $\frac{dy}{dx} = e^y$  and  $y = 0$  when  $x = 1$ , then:
- a.  $y = \ln|x|$       b.  $y = \ln|2-x|$       c.  $e^{-y} = 2-x$       d.  $y = -\ln|x|$       e.  $e^{-y} = x-2$
9. If  $\frac{dy}{dx} = \frac{x}{\sqrt{9+x^2}}$  and  $y = 5$  when  $x = 4$ , then:
- a.  $y = \sqrt{9+x^2} - 5$       b.  $y = \sqrt{9+x^2}$       c.  $y = 2\sqrt{9+x^2} - 5$
- d.  $y = \frac{\sqrt{9+x^2} + 5}{2}$       e. None of these
10. If a substance decomposes at a rate proportional to the amount of the substance present, and if the amount decreases from 40 gm to 10 gm in 2 hours, then the constant of proportionality is:
- a.  $-\ln 2$       b.  $-\frac{1}{2}$       c.  $-\frac{1}{4}$       d.  $\ln \frac{1}{4}$       e.  $\ln \frac{1}{8}$
11. A cup of coffee at temperature  $180^\circ\text{F}$  is placed on a table in a room at  $68^\circ\text{F}$ . The differential equation for its temperature at time  $t$  is  $\frac{dy}{dx} = -0.11(y-68)$ ;  $y(0) = 180$ . After 10 minutes, the temperature (in  $^\circ\text{F}$ ) of the coffee is:
- a. 96      b. 100      c. 105      d. 110      e. 115
12. Approximately how long does it take the temperature of the coffee in question 11 to drop to  $75^\circ\text{F}$ ?
- a. 10 min      b. 15 min      c. 18 min      d. 20 min      e. 25 min
13. According to Newton's law of cooling, the temperature of an object decreases at a rate proportional to the difference between its temperature and that of the surrounding air. Suppose a corpse at temperature  $32^\circ\text{C}$  arrives at a mortuary where the temperature is kept at  $10^\circ\text{C}$ . Then the differential equation satisfied by the temperature  $T$  of the corpse  $t$  hours later is:
- a.  $\frac{dT}{dt} = -k(T-10)$       b.  $\frac{dT}{dt} = k(T-32)$       c.  $\frac{dT}{dt} = 32e^{-kt}$
- d.  $\frac{dT}{dt} = -kT(T-10)$       e.  $\frac{dT}{dt} = kT(T-32)$
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14. If the corpse in Question 13 cools to  $27^\circ\text{C}$  in 1 hour, then its temperature is given by the equation:
- a.  $T = 22e^{0.205t}$       b.  $T = 10e^{1.163t}$       c.  $T = 10 + 22e^{-0.258t}$
- d.  $T = 32e^{-0.169t}$       e.  $T = 32 - 10e^{-0.093t}$
15. The population of a city increases continuously at a rate proportional, at any time, to the population at that time. The population doubles in 50 years. After 75 years, the ratio of the population  $P$  to the initial population  $P_0$  is:
- a.  $\frac{9}{4}$       b.  $\frac{5}{2}$       c.  $\frac{4}{1}$       d.  $\frac{2\sqrt{2}}{1}$       e. None of these