

1. Find the area enclosed by the parabola $y = x^2 - 3$ and the line $y = 1$.

- a) $\frac{8}{3}$ b) 32 c) $\frac{32}{3}$ d) $\frac{16}{3}$ e) none of these

2. Find the area enclosed by the parabola $y^2 = x$ and the line $x + y = 2$.

- a) $\frac{5}{2}$ b) $\frac{3}{2}$ c) $\frac{11}{6}$ d) $\frac{9}{2}$ e) $\frac{29}{6}$

3. Find the area enclosed by the curve of $y = \frac{2}{x}$ and $x + y = 3$.

- a) $\frac{1}{2} - 2\ln(2)$ b) $\frac{3}{2}$ c) $\frac{1}{2} - \ln(4)$ d) $\frac{5}{2}$ e) $\frac{3}{2} - \ln(4)$

4. Find the total area bounded by the cubic $x = y^3 - y$ and the line $x = 3y$.

- a) 4 b) $\frac{16}{3}$ c) 8 d) $\frac{32}{3}$ e) 16

5. Suppose the following is a table of values for $y = f(x)$, given that f is continuous on $[1,5]$:

x	1	2	3	4	5
y	1.62	4.15	7.50	9.00	12.13

If a trapezoidal sum is used, with $n = 4$, then the area under the curve from $x = 1$ to $x = 5$ is equal, to two decimal places, to....

- a) 6.88 b) 13.76 c) 20.30 d) 25.73 e) 27.53

6. Find the volume of the solid formed when the first quadrant region bounded by $y = x^2$, the y -axis, and $y = 4$, are revolved about the y -axis.

- a) 8π b) 4π c) $\frac{64\pi}{3}$ d) $\frac{32\pi}{3}$ e) $\frac{16\pi}{3}$

7. Find the volume of the solid formed when the region enclosed by the curves $y = x^2$ and $y = 4$ is revolved about the line $y = 4$.

- a) $\frac{256\pi}{15}$ b) $\frac{256\pi}{5}$ c) $\frac{512\pi}{5}$ d) $\frac{512\pi}{15}$ e) $\frac{64\pi}{3}$

8. The integral set-up for the volume formed when the region enclosed by the curves $y = x^2$ and $y = 4$ is revolved about the line $y = -1$ would be:

a) $4\pi \int_{-1}^4 (y+1)\sqrt{y} dy$ b) $2\pi \int_0^2 (4-x^2)^2 dx$ c) $\pi \int_{-2}^2 (16-x^4) dx$ d) $2\pi \int_0^2 (24-2x^2-x^4) dx$

e) none of these

9. The integral set-up for the volume enclosed by the curves $y = 3x - x^2$ and $y = x$ about the x -axis would be:

a) $\pi \int_0^{3/2} [(3x-x^2)^2 - x^2] dx$ b) $\pi \int_0^2 (9x^2 - 6x^3) dx$ c) $\pi \int_0^2 [(3x-x^2)^2 - x^2] dx$

d) $\pi \int_0^3 [(3x-x^2)^2 - x^4] dx$ e) $\pi \int_0^3 (2x-x^2)^2 dx$

10. The integral set-up for the volume enclosed by the curves $y = \ln(x)$, $y = 0$, and $x = e$ about the line $x = e$ would be:

a) $\pi \int_1^e (e-x)\ln(x) dx$ b) $\pi \int_0^1 (e-e^y)^2 dy$ c) $2\pi \int_1^e (e-\ln(x)) dx$

d) $\pi \int_0^e (e^2 - 2e^{y+1} + e^{2y}) dy$ e) none of these

11. The base of a solid is a circle of radius a , and every plane section perpendicular to a diameter is a square. The solid has volume

a) $\frac{8}{3}a^3$ b) $2\pi a^3$ c) $4\pi a^3$ d) $\frac{16}{3}a^3$ e) $\frac{8\pi}{3}a^3$

12. If the curves of $f(x)$ and $g(x)$ intersect for $x = a$ and $x = b$ and if $f(x) > g(x) > 0$ for all x on (a, b) , then the volume obtained when the region bounded by the curves is rotated about the x -axis is equal to

a) $\pi \int_a^b f^2(x) dx - \int_a^b g^2(x) dx$ b) $\pi \int_a^b [f(x) - g(x)]^2 dx$ c) $2\pi \int_a^b x[f(x) - g(x)] dx$

d) $\pi \int_a^b [f^2(x) - g^2(x)] dx$ e) none of these

13. Find the area enclosed by the curve of $y = \frac{4}{x^2 + 4}$, the x-axis, and the vertical lines $x = -2$ and $x = 2$.

- a) $\frac{\pi}{4}$ b) $\frac{\pi}{2}$ c) 2π d) π e) none of these

14. Find the area enclosed by the curve $y = x^3 - 2x^2 - 3x$ and the x-axis.

- a) $\frac{28}{3}$ b) $\frac{79}{6}$ c) $\frac{45}{4}$ d) $\frac{71}{6}$ e) none of these

15. The area bounded by the parabola $y = 2 - x^2$ and the line $y = x - 4$ is given by

- a) $\int_{-2}^3 (6 - x - x^2) dx$ b) $\int_{-2}^1 (2 + x + x^2) dx$ c) $\int_{-3}^2 (6 - x - x^2) dx$
d) $2 \int_0^{\sqrt{2}} (2 - x^2) dx + \int_{-3}^2 (4 - x) dx$ e) none of these

16. The volume of the solid formed when the region bounded by the curve $y = x^2$ and the line $y = 4$ is revolved around the x-axis would be:

- a) $\frac{64\pi}{5}$ b) $\frac{512\pi}{15}$ c) $\frac{256\pi}{5}$ d) $\frac{128\pi}{5}$ e) none of these

17. The volume of the solid formed when the region bounded by the curve $y = 3x - x^2$ and the line $y = 0$ is revolved around the x-axis would be:

a) $\pi \int_0^3 (9x^2 + x^4) dx$

b) $\pi \int_0^3 (3x - x^2)^2 dx$

c) $\pi \int_0^{\sqrt{3}} (3x - x^2) dx$

d) $2\pi \int_0^3 y\sqrt{9-4y} dy$

e) $\pi \int_0^{9/4} y^2 dy$

18. The base of a solid is the region bounded by the parabola $x^2 = 8y$ and the line $y = 4$, and each plane section perpendicular to the y-axis is an equilateral triangle. The volume of the solid is

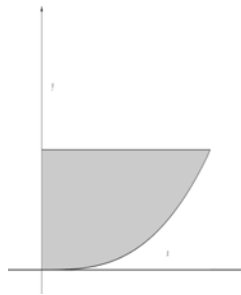
a) $\frac{64\sqrt{3}}{3}$

b) $64\sqrt{3}$

c) $32\sqrt{3}$

d) 32 e) none of these

19. The figure below shows part of the curve of and a rectangle with two vertices at $(0,0)$ and $(c,0)$. What is the ratio of the area of the rectangle to the shaded part of it above the cubic?



a) 3:4

b) 5:4

c) 4:3

d) 3:1

e) 2:1